

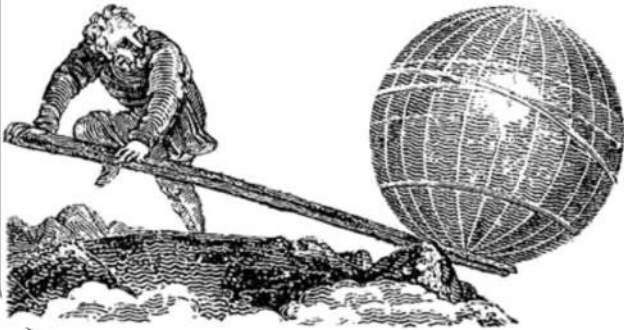
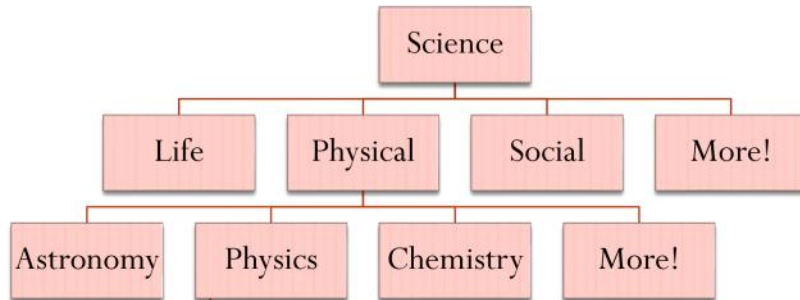
Chapter 1: General Principles

Main goals and learning objectives

- Introduce the basic ideas of *Mechanics*
- Give a concise statement of Newton's laws of motion and gravitation
- Review the principles for applying the SI system of units
- Examine standard procedures for performing numerical calculations
- Outline a general guide for solving problems



What is "statics"?



• Mechanics: Study of what happens to a "thing" when forces are applied to it

• The study of forces acting on bodies and their resulting motion, or lack of motion.

Statics: - bodies that are in static equilibrium

Mechanics

Mechanics is a branch of the physical sciences that is concerned with the **state of rest or motion of bodies that are subjected to the action of forces**

Goal for engineers:

★ Design objects that are intended to remain in static equilibrium

Rigid Bodies



Statics



Dynamics

TAM 212

Deformable Bodies



Solid Mechanics

TAM 251

Fluids



Compressible and incompressible

TAM 335



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Which forces?



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* Four fundamental forces:

1. Weak
2. strong
3. electromagnetic
4. gravitational

• Mechanics: State of rest or motion of bodies subjected **to forces**

action at a distance

attraction/repulsion

attraction

contact vs. field forces

↓
gravitational force

↓
normal force

normal force
friction force

Fundamental concepts

Basic quantities: (dimensions)

- length
- time
- mass
- force

Idealizations:

- Particle:
has mass but size is neglected
- Rigid Body:
shape of the body does not change before/after applied force
- Concentrated Force:
force applied over a small area compared to size of body



Understanding and applying these things allows for amazing achievements in engineering! (airplanes, robotics, etc)

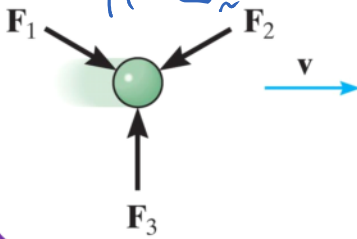
Newton's laws of motion

conservation of linear momentum, \vec{p}

First law:

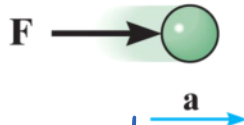
An object remains at rest or moves with constant velocity unless acted upon by a net force.

$\vec{p} = \text{const.}$
if $\sum \vec{F} = 0$



Second law: a particle acted upon by an unbalanced force \mathbf{F} experiences an acceleration \mathbf{a} that is proportional to the particle mass m :

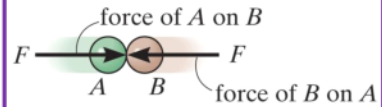
$$\sum \vec{F} = m \cdot \vec{a}$$



$$\sum \vec{F} = \frac{d}{dt} \vec{p}$$

$$= \frac{d}{dt} (m \cdot \vec{v})$$

Third law: the mutual forces of action and reaction between two particles are equal, opposite and colinear.



Newton's law of gravitational attraction

The mutual **force F of gravitation** between two particles of mass m_1 and m_2 is given by:

$$F = \frac{G \cdot m_1 \cdot m_2}{r^2}$$

G is the universal constant of gravitation (small number)
 r is the distance between the two particles

Weight is the force exerted by the earth on a particle at the earth's surface:

$$W = m \cdot \frac{G \cdot M_e}{r_e^2} = m \cdot g$$

↑
mass of particle

$$g = \frac{G \cdot M_e}{r_e^2}$$

M_e is the mass of the earth

r_e is the distance between the earth's center and the particle near the surface

g is the acceleration due to the gravity



Figure: 01_PH003
 The astronaut's weight is diminished, since she is far removed from the gravitational field of the earth.

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Units

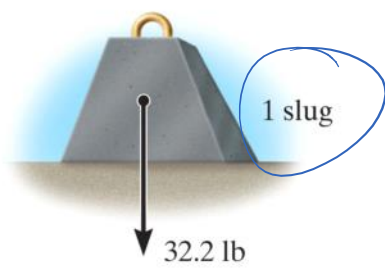
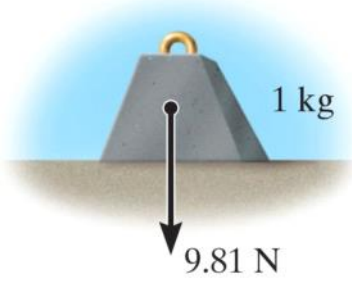
TABLE 1-1 Systems of Units

Name	Length	Time	Mass	Force
International System of Units SI	meter m	second s	kilogram kg	newton* N $(\frac{kg \cdot m}{s^2})$
U.S. Customary FPS	foot ft	second s	slug* $(\frac{lb \cdot s^2}{ft})$	pound lb

*Derived unit.

dimensions

units



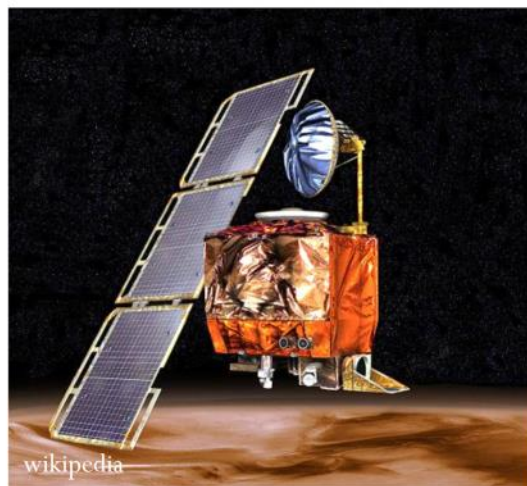
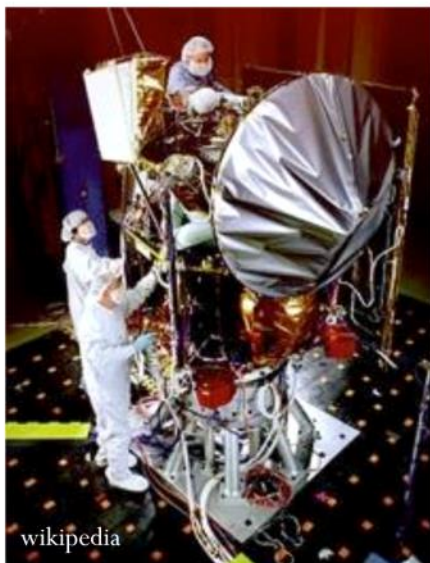
$$G = 66.73 \times 10^{-12} \frac{m^3}{kg \cdot s^2}$$

$$g = 9.81 \frac{m}{s^2}$$

$$g = 32.2 \frac{ft}{s^2}$$

Why so picky? Units matter...

- A national power company mixed up prices quoted in kilo-Watt-hour (kWh) and therms.
 - Actual price = \$50,000
 - Paid while trading on the market: \$800,000
- In Canada, a plane ran out of fuel because the pilot mistook liters for gallons! He landed the plane safely without power on an emergency airstrip.



Mars climate orbiter -- \$327.6 million

The 'super-tall' age is here: World welcomes 100th mammoth skyscraper



$h = 1400 \text{ ft}$
Approx.
9 football fields

Numerical Calculations

Dimensional Homogeneity

Equations **must** be dimensionally homogeneous, i.e., each term must be expressed in the same units. Consider the following example:



the kinematic equation
 position of a particle \downarrow

$$X(t) = v_0 \cdot t + \frac{1}{2} \cdot a_0 \cdot t^2$$

length = $\left(\frac{\text{length}}{\text{time}}\right) \text{time} + \left(\frac{\text{length}}{\text{time}^2}\right) \text{time}^2$

= length + length

Numerical Calculations

Significant figures

The number of significant figures contained in any number determines the accuracy of the number. Use 3 significant figures for final answers. For intermediate steps, use symbolic notation, store numbers in calculators or use more significant figures, in order to maintain precision.

Example 1: If $d = 3.2$ in., $w = 1.413$ in., and $h = 2.7$ in., then

